

THE
THEORY OF
DETERMINANTS
in the
HISTORICAL ORDER
OF DEVELOPMENT

VOLUME ONE

PART I. GENERAL DETERMINANTS UP TO 1841.

PART II. SPECIAL DETERMINANTS, UP TO 1841.

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PREFACE.

THE main object of this work and the contents of it will be found specified in the Introductory Chapter. It is intended for the student who aims at acquiring such a knowledge as can only be got by a study of the subject in the historical order of its development, for the investigator who is specially interested in this branch of mathematics and wishes to become acquainted with the various lines of attack opened up by previous workers, and for the general working mathematician who requires guide-books and books of reference concerning special domains.

T. M.

CAPETOWN, SOUTH AFRICA,
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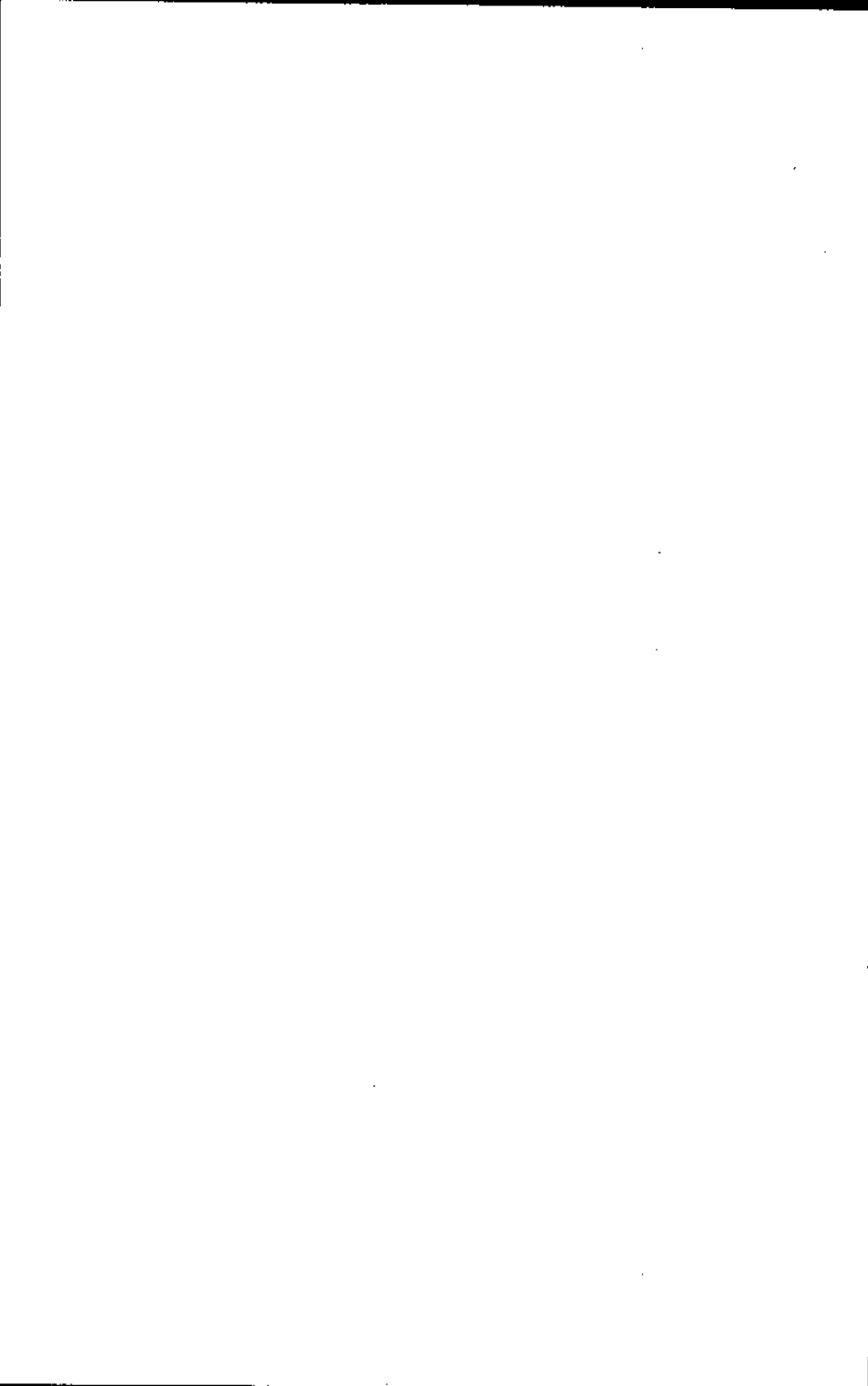
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