

SUBJECT INDEX

TO WRITINGS ON HISTORY OF DETERMINANTS

N.B.—The volumes previously published are denoted by **A**, **B**, **C**, **D**: the present volume by **Z**: other writings by *Proc. R.S.E.* and *Tr. R.S.S.A.*

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