

Haskell Modules

<http://igm.univ-mlv.fr/~vialette/?section=teaching>

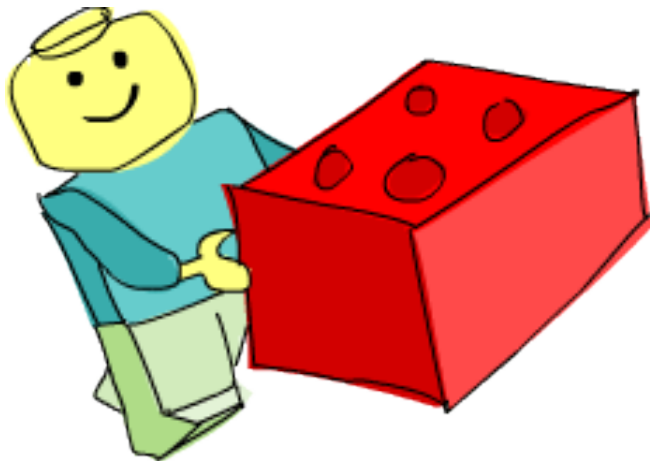
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Modules



Modules

A Haskell module is a collection of related functions, types and typeclasses.

A Haskell program is a collection of modules where the main module loads up the other modules and then uses the functions defined in them to do something.

Having code split up into several modules has quite a lot of advantages. If a module is generic enough, the functions it exports can be used in a multitude of different programs. If your own code is separated into self-contained modules which don't rely on each other too much (we also say they are loosely coupled), you can reuse them later on.

It makes the whole deal of writing code more manageable by having it split into several parts, each of which has some sort of purpose.



Modules

The Haskell standard library is split into modules, each of them contains functions and types that are somehow related and serve some common purpose.

There's a module for manipulating lists, a module for concurrent programming, a module for dealing with complex numbers, etc.

All the functions, types and typeclasses that we've dealt with so far were part of the **Prelude** module, which is imported by default.

In this chapter, we're going to examine a few useful modules and the functions that they have.



Modules

The syntax for importing modules in a Haskell script is

```
import <module name>.
```

This must be done before defining any functions, so imports are usually done at the top of the file.

One script can, of course, import several modules. Just put each import statement into a separate line.



Modules

```
import Data.List
```

```
numUniques :: (Eq a) => [a] -> Int  
numUniques = length . nub
```

When you do `import Data.List`, all the functions that `Data.List` exports become available in the global namespace, meaning that you can call them from wherever in the script.

`nub` is a function defined in `Data.List` that takes a list and weeds out duplicate elements.

Composing `length` and `nub` by doing `length . nub` produces a function that's the equivalent of `\xs -> length (nub xs)`.



Importing modules

You can also put the functions of modules into the global namespace when using GHCi. If you're in GHCi and you want to be able to call the functions exported by `Data.List`, do this:

```
Prelude> :m + Data.List  
Prelude Data.List>
```

If we want to load up the names from several modules inside GHCi, we don't have to do `:m +` several times, we can just load up several modules at once.

```
Prelude> :m + Data.List Data.Map Data.Set  
Prelude Data.List Data.Map Data.Set>
```

However, if you've loaded a script that already imports a module, you don't need to use `:m +` to get access to it.



Importing modules

If you just need a couple of functions from a module, you can selectively import just those functions.

If we wanted to import only the `nub` and `sort` functions from `Data.List`, we'd do this:

```
import Data.List (nub, sort)
```

You can also choose to import all of the functions of a module except a few select ones. That's often useful when several modules export functions with the same name and you want to get rid of the offending ones. Say we already have our own function that's called `nub` and we want to import all the functions from `Data.List` except the `nub` function:

```
import Data.List hiding (nub)
```



Importing modules

Another way of dealing with name clashes is to do qualified imports.

The `Data.Map` module, which offers a data structure for looking up values by key, exports a bunch of functions with the same name as `Prelude` functions, like `filter` or `null`.

So when we import `Data.Map` and then call `filter`, Haskell won't know which function to use.

Here's how we solve this:

```
import qualified Data.Map
```



Importing modules

```
import qualified Data.Map
```

This makes it so that if we want to reference `Data.Map`'s `filter` function, we have to do `Data.Map.filter`, whereas just `filter` still refers to the normal filter we all know (and love 😊).

But typing out `Data.Map` in front of every function from that module is kind of tedious. That's why we can rename the qualified import to something shorter:

```
import qualified Data.Map as M
```

Now, to reference `Data.Map`'s `filter` function, we just use `M.filter`.



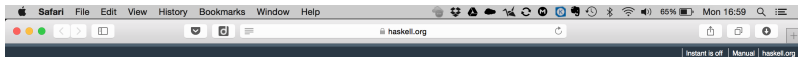
Modules

Use `https://downloads.haskell.org/~ghc/latest/docs/html/libraries/` to see which modules are in the standard library.

To search for functions or to find out where they're located, use Hoogle (`https://www.haskell.org/hoogle/`). It's a really awesome Haskell search engine, you can search by name, module name or even type signature.



Hoogle



Hoogle

Welcome to Hoogle

Links

[Haskell.org](#)
[Hackage](#)
[GHC Manual](#)
[Libraries](#)

Hoogle is a Haskell API search engine, which allows you to search many standard Haskell libraries by either function name, or by approximate type signature.

Example searches:

```
map  
(a -> b) -> [a] -> [b]  
Ord a => [a] -> [a]  
Data.Map.insert
```

Enter your own search at the top of the page.

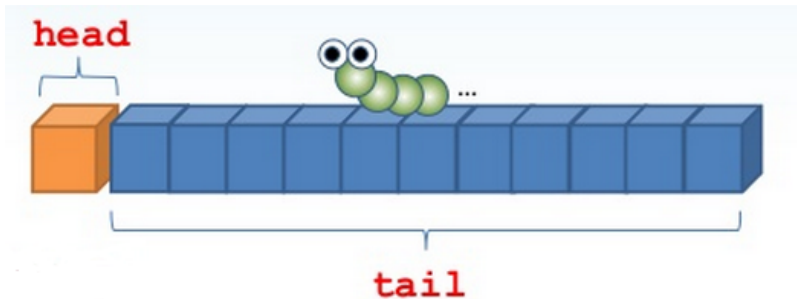
The [Hoogle manual](#) contains more details, including further details on search queries, how to install Hoogle as a command line application and how to integrate Hoogle with Firefox/Emacs/Vim etc.

I am very interested in any feedback you may have. Please [email me](#), or add an entry to my [bug tracker](#).

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Data.List



Data.List

`intersperse` takes an element and a list and then puts that element in between each pair of elements in the list.

```
Prelude Data.List> :t intersperse
intersperse :: a -> [a] -> [a]
Prelude Data.List> intersperse '.' "MONKEY"
"M.O.N.K.E.Y"
Prelude Data.List> intersperse 0 [1..10]
[1,0,2,0,3,0,4,0,5,0,6,0,7,0,8,0,9,0,10]
Prelude Data.List>
```



Data.List

`intercalate` takes a list of lists and a list. It then inserts that list in between all those lists and then flattens the result.

```
Prelude Data.List> :t intercalate
intercalate :: [a] -> [[a]] -> [a]
Prelude Data.List> intercalate " " ["hey","there","guys"]
"hey there guys"
Prelude Data.List> intercalate [0,0] [[1,2],[3,4,5],[6,7]]
[1,2,0,0,3,4,5,0,0,6,7]
Prelude Data.List>
```



Data.List

`transpose` transposes a list of lists. If you look at a list of lists as a 2D matrix, the columns become the rows and vice versa.

```
Prelude Data.List> :t transpose
transpose :: [[a]] -> [[a]]
Prelude Data.List> transpose [[1,2,3],[4,5,6],[7,8,9]]
[[1,4,7],[2,5,8],[3,6,9]]
Prelude Data.List> transpose ["hey","there","guys"]
["htg","ehu","yey","rs","e"]
Prelude Data.List>
```



Data.List

`concat` flattens a list of lists into just a list of elements.

```
Prelude Data.List> :t concat
concat :: [[a]] -> [a]
Prelude Data.List> concat ["foo","bar","car"]
"foobarcar"
Prelude Data.List> concat [[3,4,5],[2,3,4],[2,1,1]]
[3,4,5,2,3,4,2,1,1]
Prelude Data.List>
```

It will just remove one level of nesting. So if you want to completely flatten `[[[2,3],[3,4,5],[2]],[[2,3],[3,4]]]`, which is a list of lists of lists, you have to concatenate it twice.



Data.List

Doing `concatMap` is the same as first mapping a function to a list and then concatenating the list with `concat`.

```
Prelude Data.List> :t concatMap
concatMap :: (a -> [b]) -> [a] -> [b]
Prelude Data.List> concatMap (replicate 4) [1..3]
[1,1,1,1,2,2,2,2,3,3,3,3]
Prelude Data.List> concatMap (\x -> [x]) [1..3]
[1,2,3]
Prelude Data.List> concatMap (\x -> [[x]]) [1..3]
[[1],[2],[3]]
Prelude Data.List>
```



Data.List

`and` takes a list of boolean values and returns `True` only if all the values in the list are `True`.

```
Prelude Data.List> :t and
and :: [Bool] -> Bool
Prelude Data.List> and $ map (>4) [5,6,7,8]
True
Prelude Data.List> and $ map (==4) [4,4,4,3,4]
False
Prelude Data.List> and $ map ('a' `elem`) ["to", "ti", "ta"]
False
Prelude Data.List> and $ map ('t' `elem`) ["to", "ti", "ta"]
True
Prelude Data.List>
```



Data.List

`or` is like `and`, only it returns `True` if any of the boolean values in a list is `True`.

```
Prelude Data.List> :t or
or :: [Bool] -> Bool
Prelude Data.List> or $ map (==4) [2,3,4,5,6,1]
True
Prelude Data.List> or $ map (>4) [1,2,3]
False
Prelude Data.List>
```



Data.List

`any` and `all` take a predicate and then check if any or all the elements in a list satisfy the predicate, respectively. Usually we use these two functions instead of mapping over a list and then doing `and` or `or`.

```
Prelude Data.List> :t any
any :: (a -> Bool) -> [a] -> Bool
Prelude Data.List> any (==4) [2,3,5,6,1,4]
True
Prelude Data.List> any (`elem` ['A'..'Z']) "HEYGUYSwhatsup"
True
Prelude Data.List> :t all
all :: (a -> Bool) -> [a] -> Bool
Prelude Data.List> all (>4) [6,9,10]
True
Prelude Data.List> all (`elem` ['A'..'Z']) "HEYGUYSwhatsup"
False
Prelude Data.List>
```



Data.List

`iterate` takes a function and a starting value. It applies the function to the starting value, then it applies that function to the result, then it applies the function to that result again, etc. It returns all the results in the form of an infinite list.

```
Prelude Data.List> :t iterate
iterate :: (a -> a) -> a -> [a]
Prelude Data.List> take 10 $ iterate (*2) 1
[1,2,4,8,16,32,64,128,256,512]
Prelude Data.List> take 3 $ iterate (++) "haha" "haha"
["haha","hahahaha","hahahahahahaha"]
Prelude Data.List>
```



Data.List

`splitAt` takes a number and a list. It then splits the list at that many elements, returning the resulting two lists in a tuple.

```
Prelude Data.List> :t splitAt
splitAt :: Int -> [a] -> ([a], [a])
Prelude Data.List> splitAt 3 "heyman"
("hey","man")
Prelude Data.List> splitAt 100 "heyman"
("heyman","")
Prelude Data.List> splitAt (-3) "heyman"
("", "heyman")
Prelude Data.List> let (a,b) = splitAt 3 "foobar" in b ++ a
"barfoo"
Prelude Data.List>
```



Data.List

`takeWhile` is a really useful little function. It takes elements from a list while the predicate holds and then when an element is encountered that doesn't satisfy the predicate, it's cut off. It turns out this is very useful.

```
Prelude Data.List> :t takeWhile
takeWhile :: (a -> Bool) -> [a] -> [a]
Prelude Data.List> takeWhile (>3) [6,5,4,3,2,1,2,3,4,5,4,3,2,1]
[6,5,4]
Prelude Data.List> takeWhile (/=' ') "This is a sentence"
"This"
Prelude Data.List> sum $ takeWhile (<10000) $ map (^3) [1..]
53361
Prelude Data.List>
```



Data.List

`dropWhile` is similar to `takeWhile`, only it drops all the elements while the predicate is true. Once predicate equates to `False`, it returns the rest of the list. An extremely useful (and lovely 😊) function!

```
Prelude Data.List> :t dropWhile
dropWhile :: (a -> Bool) -> [a] -> [a]
Prelude Data.List> dropWhile (/=' ') "This is a sentence"
" is a sentence"
Prelude Data.List> dropWhile (<3) [1,2,2,2,3,4,5,4,3,2,1]
[3,4,5,4,3,2,1]
Prelude Data.List> :{
Prelude Data.List| let stock = [(9.2,2008,01),(11.4,2008,02),
Prelude Data.List|                                     (7.2,2007,03)]
Prelude Data.List| :}
Prelude Data.List> head $ dropWhile (\(v,y,n) -> v < 10) stock
(11.4,2008,2)
Prelude Data.List>
```



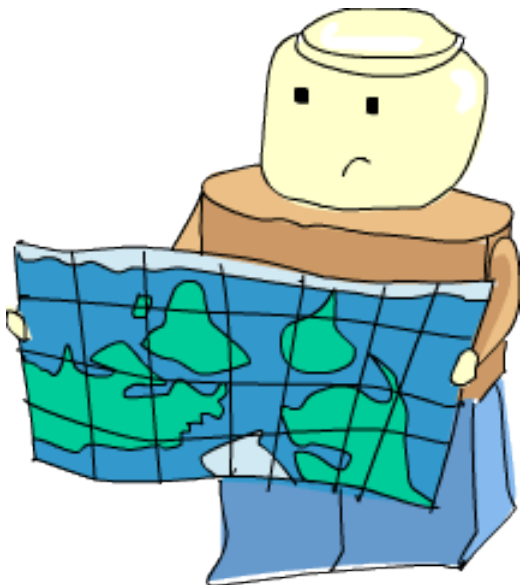
Data.List

`sort` simply sorts a list. The type of the elements in the list has to be part of the `Ord` typeclass, because if the elements of a list can't be put in some kind of order, then the list can't be sorted.

```
Prelude Data.List> :t sort
sort :: Ord a => [a] -> [a]
Prelude Data.List> sort [8,5,3,2,1,6,4,2]
[1,2,2,3,4,5,6,8]
Prelude Data.List> sort ['a','g','d','b','d','c','f','e',]
<interactive>:204:39: parse error on input ']'
Prelude Data.List> sort ['a','g','d','b','d','c','f','e']
"abcddefg"
Prelude Data.List>
```



Data.Map



Data.Map

Association lists (also called dictionaries) are lists that are used to store key-value pairs where ordering doesn't matter.

For instance, we might use an association list to store phone numbers, where phone numbers would be the values and people's names would be the keys. We don't care in which order they're stored, we just want to get the right phone number for the right person.

```
phoneBook =  
  [("betty", "555-2938")  
   , ("bonnie", "452-2928")  
   , ("patsy", "493-2928")  
   , ("lucille", "205-2928")  
   , ("wendy", "939-8282")  
   , ("penny", "853-2492")  
  ]
```



Data.Map

Let's make a function that looks up some value given a key.

```
findKey :: (Eq k) => k -> [(k,v)] -> v
findKey k = snd . head . filter (\(k',v) -> k'==k)
```

Here, if a key isn't in the association list, we'll end up trying to get the head of an empty list, which throws a runtime error. However, we should avoid making our programs so easy to crash, so let's use the Maybe data type. If we don't find the key, we'll return a **Nothing**. If we find it, we'll return **Just** something, where something is the value corresponding to that key.

```
findKey :: (Eq k) => k -> [(k,v)] -> Maybe v
findKey key [] = Nothing
findKey k ((k',v):xs) = if k == k'
                        then Just v
                        else findKey k xs
```



Data.Map

```
findKey :: (Eq k) => k -> [(k,v)] -> Maybe v  
findKey k = foldr (\(k',v) acc -> if k==k' then Just v else acc) Nothing
```

It's usually better to use folds for this standard list recursion pattern instead of explicitly writing the recursion because they're easier to read and identify. Everyone knows it's a fold when they see the foldr call, but it takes some more thinking to read explicit recursion.



Data.Map

```
ghci> findKey "penny" phoneBook
Just "853-2492"
ghci> findKey "betty" phoneBook
Just "555-2938"
ghci> findKey "wilma" phoneBook
Nothing
```

We just implemented the `lookup` function from `Data.List`.

If we want to find the corresponding value to a key, we have to traverse all the elements of the list until we find it.

The `Data.Map` module offers association lists that are much faster (because they're internally implemented with trees) and also it provides a lot of utility functions.



Data.Map

Because `Data.Map` exports functions that clash with the `Prelude` and `Data.List` ones, we'll do a qualified import.

```
import qualified Data.Map as Map
```



Data.Map

The `fromList` function takes an association list (in the form of a list) and returns a map with the same associations.

```
Prelude Map> :t Map.fromList
Map.fromList :: Ord k => [(k, a)] -> Map.Map k a
Prelude Map> Map.fromList [('a', 1), ('b', 2), ('c', 3), ('d', 4)]
fromList [('a', 1), ('b', 2), ('c', 3), ('d', 4)]
Prelude Map> Map.fromList [(i, i^2) | i <- [1..5]]
fromList [(1, 1), (2, 4), (3, 9), (4, 16), (5, 25)]
Prelude Map> Map.fromList [(1, 1), (1, 1), (2, 2)]
fromList [(1, 1), (2, 2)]
Prelude Map>
```



Data.Map

`empty` represents an empty map. It takes no arguments, it just returns an empty map.

```
Prelude Map> :t Map.empty
Map.empty :: Map.Map k a
Prelude Map> Map.empty
fromList []
Prelude Map>
```



Data.Map

insert

`insert` takes a key, a value and a map and returns a new map that's just like the old one, only with the key and value inserted.

```
Prelude Map> :t Map.insert
Map.insert :: Ord k => k -> a -> Map.Map k a -> Map.Map k a
Prelude Map> Map.insert 'a' 1 Map.empty
fromList [('a',1)]
Prelude Map> Map.insert 'a' 1 $ Map.insert 'b' 2 Map.empty
fromList [('a',1),('b',2)]
Prelude Map> let m = Map.empty
Prelude Map> Map.insert 'a' 1 $ Map.insert 'b' 2 m
fromList [('a',1),('b',2)]
Prelude Map>
```



Data.Map

insert

We can implement our own `fromList` by using the empty map, insert and a fold.

```
fromList' :: (Ord k) => [(k,v)] -> Map.Map k v  
fromList' = foldr (\(k,v) acc -> Map.insert k v acc) Map.empty
```

It's a pretty straightforward fold. We start of with an empty map and we fold it up from the right, inserting the key value pairs into the accumulator as we go along.



Data.Map

`null`

`null` checks if a map is empty.

```
Prelude Map> :t Map.null
Map.null :: Map.Map k a -> Bool
Prelude Map> Map.null Map.empty
True
Prelude Map> Map.null $ Map.insert "k" "v" Map.empty
False
Prelude Map>
```



Data.Map

size

size reports the size of a map.

```
Prelude Map> :t Map.size
Map.size :: Map.Map k a -> Int
Prelude Map> Map.size Map.empty
0
Prelude Map> Map.size $ Map.insert "k" "v" Map.empty
1
Prelude Map>
```



Data.Map

singleton

`singleton` takes a key and a value and creates a map that has exactly one mapping.

```
Prelude Map> :t Map.singleton
Map.singleton :: k -> a -> Map.Map k a
Prelude Map> Map.singleton 3 9
fromList [(3,9)]
Prelude Map> Map.insert 5 9 $ Map.singleton 3 9
fromList [(3,9),(5,9)]
Prelude Map>
```



Data.Map

lookup

`lookup` works like the `Data.List lookup`, only it operates on maps. It returns `Just` something if it finds something for the key and `Nothing` if it doesn't.

```
Prelude Map> :t Map.lookup
Map.lookup :: Ord k => k -> Map.Map k a -> Maybe a
Prelude Map> let m = Map.insert 5 9 $ Map.singleton 3 9
Prelude Map> Map.lookup 5 m
Just 9
Prelude Map> Map.lookup 6 m
Nothing
Prelude Map>
```



Data.Map

member

`member` is a predicate takes a key and a map and reports whether the key is in the map or not.

```
Prelude Map> :t Map.member
Map.member :: Ord k => k -> Map.Map k a -> Bool
Prelude Map> let m = Map.insert 5 9 $ Map.singleton 3 9
Prelude Map> Map.member 5 m
True
Prelude Map> Map.member 6 m
False
Prelude Map>
```



Data.Map

map and filter

map and filter work much like their list equivalents.

```
Prelude Map> let m = Map.fromList [(1,1),(2,4),(3,9)]
Prelude Map> :t Map.map
Map.map :: (a -> b) -> Map.Map k a -> Map.Map k b
Prelude Map> Map.map (*100) m
fromList [(1,100),(2,400),(3,900)]
Prelude Map> :t Map.filter
Map.filter :: (a -> Bool) -> Map.Map k a -> Map.Map k a
Prelude Map> Map.filter (>2) m
fromList [(2,4),(3,9)]
Prelude Map>
```



Data.Map

toList

fromList is the inverse of fromList.

```
Prelude Map> :t Map.toList
Map.toList :: Map.Map k a -> [(k, a)]
Prelude Map> Map.toList . Map.insert 9 2 $ Map.singleton 4 3
[(4,3),(9,2)]
Prelude Map> Map.toList Map.empty
[]
Prelude Map>
```



Data.Map

keys and elems

`keys` and `elems` return lists of keys and values respectively. `keys` is the equivalent of `map fst . Map.toList` and `elems` is the equivalent of `map snd . Map.toList`.

```
Prelude Map> :t Map.keys
Map.keys :: Map.Map k a -> [k]
Prelude Map> :t Map.elems
Map.elems :: Map.Map k a -> [a]
Prelude Map> Map.keys $ Map.insert 9 2 $ Map.singleton 4 3
[4,9]
Prelude Map> Map.elems $ Map.insert 9 2 $ Map.singleton 4 3
[3,2]
Prelude Map>
```



Data.Set

The `Data.Set` module offers us, well, sets.

Sets are kind of like a cross between lists and maps. All the elements in a set are unique. And because they're internally implemented with trees (much like maps in `Data.Map`), they're ordered.

Checking for membership, inserting, deleting, etc. is much faster than doing the same thing with lists.

The most common operation when dealing with sets are inserting into a set, checking for membership and converting a set to a list.

Because the names in `Data.Set` clash with a lot of `Prelude` and `Data.List` names, we do a qualified import (e.g.,



```
import qualified Data.Set as Set).
```



Data.Set

fromList

The `fromList` function works much like you would expect. It takes a list and converts it into a set.

```
ghci> :t Set.fromList
Set.fromList :: Ord a => [a] -> Data.Set.Set a
ghci> Set.fromList []
fromList []
ghci> Set.fromList "i'm a poor lonesome cowboy"
fromList " 'abceilmnoprsyw"
ghci>
```



Data.Set

intersection

Use `intersection` function to see which elements sets both share.

```
ghci> let set1 = Set.fromList "To be or not to Be"
ghci> let set2 = Set.fromList "That is the question"
ghci> :t Set.intersection
Set.intersection
  :: Ord a => Data.Set.Set a -> Data.Set.Set a -> Data.Set.Set a
ghci> Set.intersection set1 set2
fromList " Tenot"
ghci>
```



Data.Set

difference

We can use the `difference` function to see which letters are in the first set but aren't in the second one and vice versa.

```
ghci> let set1 = Set.fromList "To be or not to Be"
ghci> let set2 = Set.fromList "That is the question"
ghci> :t Set.difference
Set.difference
  :: Ord a => Data.Set.Set a -> Data.Set.Set a -> Data.Set.Set a
ghci> Set.difference set1 set2
fromList "Bbr"
ghci> Set.difference set2 set1
fromList "ahiqsu"
ghci>
```



Data.Set

union

we can see all the unique letters used in both sentences by using `union`.

```
ghci> let set1 = Set.fromList "To be or not to Be"
ghci> let set2 = Set.fromList "That is the question"
ghci> :t Set.union
Set.union
  :: Ord a => Data.Set.Set a -> Data.Set.Set a -> Data.Set.Set a
ghci> Set.union set1 set2
fromList " BTabehinoqrstu"
ghci>
```



Data.Set

`null, size, ...`

The `null`, `size`, `member`, `empty`, `singleton`, `insert` and `delete` functions all work like you'd expect them to.

```
ghci> :t Set.null
Set.null :: Data.Set.Set a -> Bool
ghci> :t Set.empty
Set.empty :: Data.Set.Set a
ghci> Set.null Set.empty
True
ghci>
```



Data.Set

`null, size, ...`

The `null`, `size`, `member`, `empty`, `singleton`, `insert` and `delete` functions all work like you'd expect them to.

```
ghci> Set.null $ Set.fromList [3,4,5,5,4,3]
False
ghci> :t Set.size
Set.size :: Data.Set.Set a -> Int
ghci> Set.size $ Set.fromList [3,4,5,3,4,5]
3
ghci>
```



Data.Set

`null, size, ...`

The `null`, `size`, `member`, `empty`, `singleton`, `insert` and `delete` functions all work like you'd expect them to.

```
ghci> :t Set.singleton
Set.singleton :: a -> Data.Set.Set a
ghci> Set.singleton 9
fromList [9]
ghci> Set.null $ Set.singleton 9
False
ghci> Set.size $ Set.singleton 9
1
ghci>
```



Data.Set

`null, size, ...`

The `null`, `size`, `member`, `empty`, `singleton`, `insert` and `delete` functions all work like you'd expect them to.

```
ghci> :t Set.insert
Set.insert :: Ord a => a -> Data.Set.Set a -> Data.Set.Set a
ghci> Set.insert 4 $ Set.fromList [9,3,8,1]
fromList [1,3,4,8,9]
ghci> Set.insert 8 $ Set.fromList [5..10]
fromList [5,6,7,8,9,10]
ghci> Set.insert 8 $ Set.fromList [5..10]
```



Data.Set

`null, size, ...`

The `null`, `size`, `member`, `empty`, `singleton`, `insert` and `delete` functions all work like you'd expect them to.

```
ghci> :t Set.delete
Set.delete :: Ord a => a -> Data.Set.Set a -> Data.Set.Set a
ghci> Set.delete 4 $ Set.fromList [3,4,5,4,3,4,5]
fromList [3,5]
ghci> Set.delete 1 $ Set.fromList [3,4,5,4,3,4,5]
fromList [3,4,5]
ghci>
```



Data.Set

`isSubsetOf` and `isProperSubsetOf`

We can also check for subsets or proper subset. Set A is a **subset** of set B if B contains all the elements that A does. Set A is a **proper subset** of set B if B contains all the elements that A does but has more elements.

```
ghci> :t Set.isSubsetOf
Set.isSubsetOf :: Ord a => Data.Set.Set a -> Data.Set.Set a -> Bool
ghci> :t Set.isProperSubsetOf
Set.isProperSubsetOf
  :: Ord a => Data.Set.Set a -> Data.Set.Set a -> Bool
ghci> Set.fromList [2,3,4] `Set.isSubsetOf` Set.fromList [1,2,3,4,5]
True
ghci> Set.fromList [1,2,3,4,5] `Set.isSubsetOf` Set.fromList [1,2,3,4,5]
True
ghci> Set.fromList [1,2,3,4,5] `Set.isProperSubsetOf` Set.fromList [1,2,3,4,5]
False
ghci> Set.fromList [2,3,4,8] `Set.isSubsetOf` Set.fromList [1,2,3,4,5]
False
ghci>
```



Data.Set

map and filter

We can also `map` over sets and `filter` them.

```
ghci> :t Set.map
Set.map :: Ord b => (a -> b) -> Data.Set.Set a -> Data.Set.Set b
ghci> Set.map (+1) $ Set.fromList [3,4,5,6,7,2,3,4]
fromList [3,4,5,6,7,8]
ghci> :t Set.filter
Set.filter :: (a -> Bool) -> Data.Set.Set a -> Data.Set.Set a
ghci> Set.filter odd $ Set.fromList [3,4,5,6,7,2,3,4]
fromList [3,5,7]
ghci>
```



Data.Set

Sets are often used to weed a list of duplicates from a list by first making it into a set with `fromList` and then converting it back to a list with `toList`.

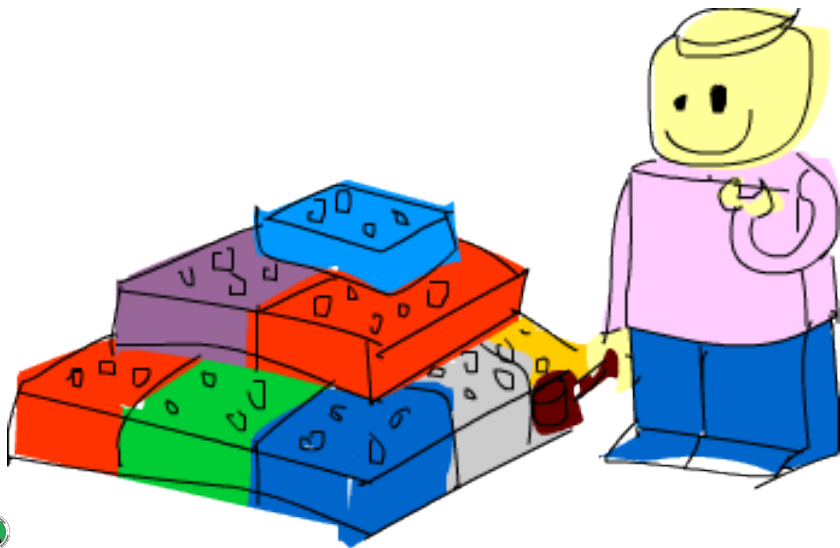
The `Data.List` function `nub` already does that, but weeding out duplicates for large lists is much faster if you cram them into a set and then convert them back to a list than using `nub`.

But using `nub` only requires the type of the list's elements to be part of the `Eq` typeclass, whereas if you want to cram elements into a set, the type of the list has to be in `Ord`.

```
ghci> let setNub xs = Set.toList $ Set.fromList xs
ghci> setNub "HEY WHATS CRACKALACKIN"
" ACEHIKLNIRSTWY"
ghci> import Data.List as List
ghci> List.nub "HEY WHATS CRACKALACKIN"
"HEY WATSCRKLIN"
ghci>
```



Making you own module



Making you own module

At the beginning of a module, we specify the module name.

If we have a file called `Geometry.hs`, then we should name our module `Geometry`. Then, we specify the functions that it exports and after that, we can start writing the functions.

```
module Geometry
( sphereVolume
, sphereArea
, cubeVolume
, cubeArea
, cuboidArea
, cuboidVolume
) where

...
```



Making you own module

```
sphereVolume :: Float -> Float
sphereVolume radius = (4.0 / 3.0) * pi * (radius ^ 3)

sphereArea :: Float -> Float
sphereArea radius = 4 * pi * (radius ^ 2)

cubeVolume :: Float -> Float
cubeVolume side = cuboidVolume side side side

cubeArea :: Float -> Float
cubeArea side = cuboidArea side side side

cuboidVolume :: Float -> Float -> Float -> Float
cuboidVolume a b c = rectangleArea a b * c

cuboidArea :: Float -> Float -> Float -> Float
cuboidArea a b c = rectangleArea a b * 2 + rectangleArea a c * 2 +
                    rectangleArea c b * 2

-- not exported
rectangleArea :: Float -> Float -> Float
rectangleArea a b = a * b
```



Making you own module

When making a module, we usually export only those functions that act as a sort of interface to our module so that the implementation is hidden.

If someone is using our **Geometry** module, they don't have to concern themselves with functions that we don't export.

We can decide to change those functions completely or delete them in a newer version (we could delete **rectangleArea** and just use `*` instead) and no one will mind because we weren't exporting them in the first place.



Making you own module

To use our module:

```
import Geometry
```

or

```
import qualified Geometry
```

or

```
import qualified Geometry as G
```

Geometry.hs has to be in the same folder that the program that's importing it is in, though.



Making you own module

Modules can also be given a hierarchical structures.

Each module can have a number of sub-modules and they can have sub-modules of their own.

Let's section these functions off so that **Geometry** is a module that has three sub-modules, one for each type of object.

First, we'll make a folder called Geometry. Mind the capital G. In it, we'll place three files: `Sphere.hs`, `Cuboid.hs`, and `Cube.hs`.



Making you own module

Sphere.hs

```
module Geometry.Sphere
```

```
( volume
```

```
, area
```

```
) where
```

```
volume :: Float -> Float
```

```
volume radius = (4.0 / 3.0) * pi * (radius ^ 3)
```

```
area :: Float -> Float
```

```
area radius = 4 * pi * (radius ^ 2)
```



Making you own module

Cuboid.hs

```
module Geometry.Cuboid
```

```
( volume
```

```
, area
```

```
) where
```

```
volume :: Float -> Float -> Float -> Float
```

```
volume a b c = rectangleArea a b * c
```

```
area :: Float -> Float -> Float -> Float
```

```
area a b c = rectangleArea a b * 2 + rectangleArea a c * 2  
            rectangleArea c b * 2
```

```
rectangleArea :: Float -> Float -> Float
```

```
rectangleArea a b = a * b
```



Making you own module

Cube.hs

```
module Geometry.Cube
( volume
, area
) where

import qualified Geometry.Cuboid as Cuboid

volume :: Float -> Float
volume side = Cuboid.volume side side side

area :: Float -> Float
area side = Cuboid.area side side side
```



Making you own module

So now if we're in a file that's on the same level as the Geometry folder, we can do, say:

```
import Geometry.Sphere
```

If we want to juggle two or more of these modules, we have to do qualified imports because they export functions with the same names. So we just do something like:

```
import qualified Geometry.Sphere as Sphere
import qualified Geometry.Cuboid as Cuboid
import qualified Geometry.Cube as Cube
```

